A new strategy for polarization calibration of VLBI data



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Polarimetry with VLBI

Theory & Simulation



→ VLBI Polarimetry

Polarimetry with VLBI



Observed Voltages

$$V_L = G_L(E_L + D_L E_R e^{-2i\phi})$$

$$V_R = G_R(E_R + D_R E_L e^{2i\phi})$$



Observed Voltages

$$V_L = G_L(E_L + D_L E_R e^{-2i\phi})$$

$$V_R = G_R(E_R + D_R E_L e^{2i\phi})$$
'Correct' source signal

'Instrumental' polarization (often called "D-Terms")

: a fraction of the signal from the opposite polarization is 'leaked' \rightarrow needs to be properly calibrated.

$$V_{L} = G_{L}(E_{L} + D_{L}E_{R}e^{-2i\phi})$$

$$V_{R} = G_{R}(E_{R} + D_{R}E_{L}e^{2i\phi})$$

$$\downarrow$$

$$R_{i}L_{j} = G_{iR}G_{jL}^{*}\left(P_{ij} + D_{iR}Ie^{2i\phi_{i}} + D_{jL}^{*}Ie^{2i\phi_{j}} + D_{iR}D_{jL}^{*}P_{ij}^{*}e^{2i(\phi_{i} + \phi_{j})}\right)$$

$$L_{i}R_{j} = G_{iL}G_{jR}^{*}\left(P_{ij}^{*} + D_{iL}Ie^{-2i\phi_{i}} + D_{jR}^{*}Ie^{-2i\phi_{j}} + D_{iL}D_{jR}^{*}P_{ij}e^{-2i(\phi_{i} + \phi_{j})}\right)$$

$$V_{L} = G_{L}(E_{L} + D_{L}E_{R}e^{-2i\phi})$$
Cross-hand visibilities
$$V_{R} = G_{R}(E_{R} + D_{R}E_{L}e^{2i\phi})$$

$$\downarrow$$

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$$V_{L} = G_{L}(E_{L} + D_{L}E_{R}e^{-2i\phi})$$

$$V_{R} = G_{R}(E_{R} + D_{R}E_{L}e^{2i\phi})$$

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Source-intrinsic signal





AIPS task LPCAL : a conventional calibration tool



LPCAL can fit the model to 'a single source' visibility data



1. There are often not many scans for 'long baseline antennas'. \rightarrow D-term estimation accuracy is limited for those antennas.

NRA0530 1055+018 **3C273** 3C279 **OJ287** 3C120 NRA0150 3C84 **3C345 CTA102** 3C454.3 15^h 10^h 05^h 20^h 01^h UT starting on Tue 20 Feb 2018

LPCAL can fit the model to 'a single source' visibility data

2. When we have a small number of antennas (such as the KVN).

 \rightarrow difficult to determine which source is 'the best calibrator'?

LPCAL ignores the 2nd order terms.

$$\begin{split} \tilde{r}_{ij}^{RL}(u,v) &= \sum_{s} p_{s}F_{s}(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_{i}} + D_{jL}^{*}r_{ij}^{RR}(u,v)e^{2i\phi_{j}} + \sum_{s} p_{s}^{*}F_{s}(u,v)D_{iL}D_{jL}^{*}e^{2i(\phi_{i}+\phi_{j})} \\ \tilde{r}_{ij}^{LR}(u,v) &= \sum_{s} p_{s}^{*}F_{s}(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_{i}} + D_{jR}^{*}r_{ij}^{LL}(u,v)e^{-2i\phi_{j}} + \sum_{s} p_{s}F_{s}(u,v)D_{iL}D_{jR}^{*}e^{-2i(\phi_{i}+\phi_{j})} \\ Ignore \end{split}$$

3. When the D-terms are large and source polarization is large \rightarrow cannot ignore the 2nd order terms.



4. When antennas have quite different sensitivities (e.g., ALMA + EHT, GBT + VLBA)
→ We must properly take antenna weights into account (not possible for LPCAL).

$$\tilde{r}_{ij}^{RL}(u,v) = \sum_{s} p_{s}F_{s}(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_{i}} + D_{jL}^{*}r_{ij}^{RR}(u,v)e^{2i\phi_{j}} + \sum_{s} p_{s}^{*}F_{s}(u,v)D_{iR}D_{jL}^{*}e^{2i(\phi_{i}+\phi_{j})}$$

$$\tilde{r}_{ij}^{LR}(u,v) = \sum_{s} p_{s}^{*}F_{s}(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_{i}} + D_{jR}^{*}r_{ij}^{LL}(u,v)e^{-2i\phi_{j}} + \sum_{s} p_{s}F_{s}(u,v)D_{iL}D_{jR}^{*}e^{-2i(\phi_{i}+\phi_{j})}$$

Let's develop a new algorithm which fits the model to 'multiple sources' visibilities simultaneously.

Possible advantages are

(i) increase in 'effective' signal-to-noise ratio (we have more data points).
(ii) improvement of the D-term accuracy thanks to the 2nd order terms included.
(iii) less efforts and time required (no need to figure out which calibrator is the best)
(iv) controlling weights for different antennas and sources are flexible (which might be important for the EHT).



All these processes can be done by running a single script. It takes a few minutes to less than 15 minutes depending on the data size

VLBA



Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$

VLBA



Los Alamos – Pie Town

Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$

VLBA



Mauna Kea – Saint Croix

Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$

HSA



Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$

Does it work well?

KaVA (5 Stations)





Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$

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KVN



Tamna – Yonsei

Circles : LHS (data) $\tilde{r}_{ij}^{RL}(u,v) = pF(u,v) + D_{iR}r_{ij}^{LL}(u,v)e^{2i\phi_i} + D_{jL}^*r_{ij}^{RR}(u,v)e^{2i\phi_j} + p^*F(u,v)D_{iR}D_{jL}^*e^{2i(\phi_i+\phi_j)}$ Magenta : RHS (model) $\tilde{r}_{ij}^{LR}(u,v) = p^*F(u,v) + D_{iL}r_{ij}^{RR}(u,v)e^{-2i\phi_i} + D_{jR}^*r_{ij}^{LL}(u,v)e^{-2i\phi_j} + pF(u,v)D_{iL}D_{jR}^*e^{-2i(\phi_i+\phi_j)}$









— A new algorithm for polarization calibration of VLBI data has been developed. Which advantages does it have?

- (i) It increases effective signal to noise ratio and improves the calibration accuracy. \rightarrow powerful for studying low-polarization sources (such as M87!).
- (ii) It will solve the problem of global VLBI arrays that there is not much common sky for a single source.
 - \rightarrow will be important for on-going and future global VLBI studies by using GMVA + ALMA, EHT + ALMA, and satellite missions.
- (iii) It is easy to use (you can just run a single script).
 - \rightarrow Don't spend much time to figure out which calibrator is the best. You can use all!
- (iv) It will be very effective for future KVN polarization observations where we have a small number of baselines but usually have many different sources observed.

 \rightarrow You can do a unique science with the KVN (linear polarization and Rotation Measure analysis at 2 ~ 3 mm).

Please use my code for your studies!

AIPS task LPCAL : a conventional calibration tool



There is almost no astronomical object having a constant polarization across its structure.





Assume a constant fractional polarization for the CLEAN components in each 'box'

AIPS task LPCAL : a conventional calibration tool



Assume a 'constant fractional polarization' for each source sub-components

Does it work well?



When ignoring the 2^{nd} order terms and comparing with the LPCAL result, they are consistent within $\sim 10^{-4}$ levels.

Does it work well?



When ignoring the 2^{nd} order terms and comparing with the LPCAL result, they are consistent within $\sim 10^{-4}$ levels.







If the multi-source fitting code works well, then the results must be consistent with the single-source fitting results (because OJ 287 and OQ 208 are good calibrators). \rightarrow This is the case!